

# Subsurface Pressure and Stress

Geol493K

## Stress

Stress = force / area  
 Units = Pascals, psi

= N/m<sup>2</sup>  
 = kg/(m · s<sup>2</sup>)



Force = 50 kg \* 9.8 m/s<sup>2</sup>  
 Area = 1 cm<sup>2</sup> = 0.0001 m<sup>2</sup>  
 Stress = 4,900,000 Pascals  
 686 psi

## How much is 1 Pascal?

- 1 Pa = 0.00014 psi
- Car tire ~230,000 Pa
- 1 Megapascal (1 MPa) = 1 million Pa  
 = 1 x 10<sup>6</sup> Pa  
 = 145 psi

## Stress/pressure

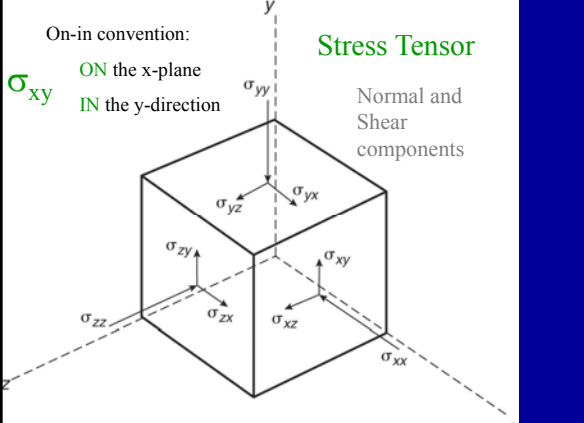
- What is the difference?
- Pressure - Scalar quantity
- Stress - Tensor quantity
- Pressure – in fluids
- Stress – in solid bodies

On-in convention:

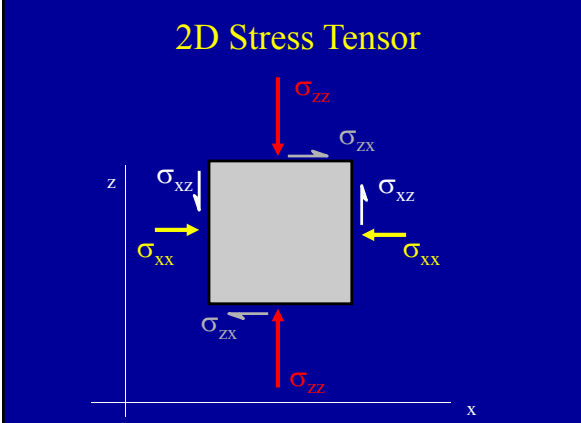
$\sigma_{xy}$  ON the x-plane  
 IN the y-direction

### Stress Tensor

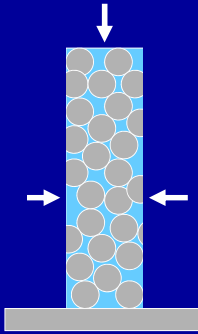
Normal and Shear components



## 2D Stress Tensor



## Lithostatic stress/ hydrostatic stress



- Lithostatic stress
- Tectonic stress
- Fluid Pressure
  - Hydrostatic
  - Hydrodynamic

## Lithostatic Stress

- Due to load of overburden
- Magnitude of stress components is the same in all directions

$$\sigma_{\text{Lith}} = \rho \cdot g \cdot Z$$

↑ gravity  
 ↓ density  
 ← depth

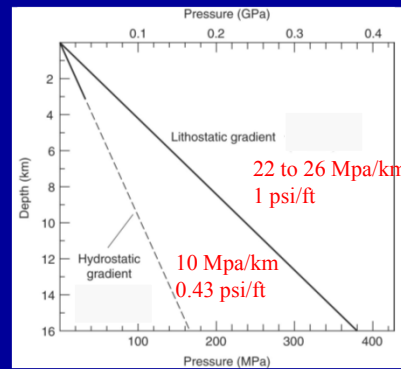
## Lithostatic Stress Gradient

$$\sigma_{\text{Lith}} = \rho \cdot g \cdot z$$

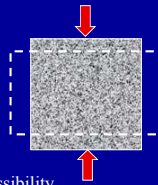
Rock density= 2000 to 3000 kg/ m<sup>3</sup>

$$\begin{aligned} \sigma_{\text{Lith}} &= 2500 \text{ kg/ m}^3 \times 9.8 \text{ m/ s}^2 \times 1000 \text{ m} \\ &\approx 25 \text{ MPa/km} \\ &\approx 1 \text{ psi/ft} \end{aligned}$$

## Pressure/stress gradients



## What about horizontal stress?



Rocks are elastic solids  
Horizontal stress depends on rock compressibility

Poisson's Ratio  $\nu = | -\epsilon_{yy} / \epsilon_{xx} |$

$\nu = 0.5$  incompressible material (no volume loss)

Rocks  $\nu = 0.1$  to  $0.3$

## Horizontal Stress

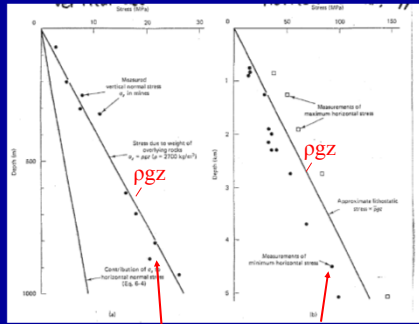
$$\sigma_{\text{Hor}} = [\nu / (1 - \nu)] \rho \cdot g \cdot z$$

If  $\nu = 0.5$ ,  $\sigma_{\text{Hor}} = \rho \cdot g \cdot z$

If  $\nu = 0.25$ ,  $\sigma_{\text{Hor}} = 0.33 \rho \cdot g \cdot z$

Horizontal stress is about 1/3 of vertical if rocks are lithified

## Comparison of vertical and horizontal stresses

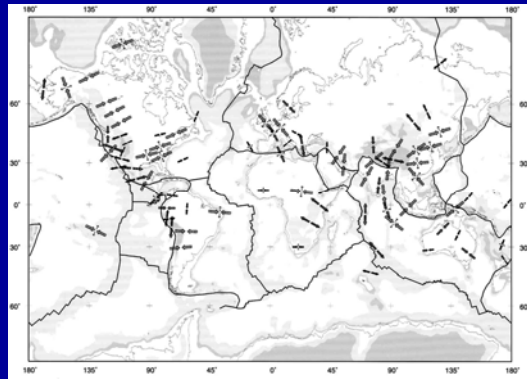


Suppe, 1985

Vertical

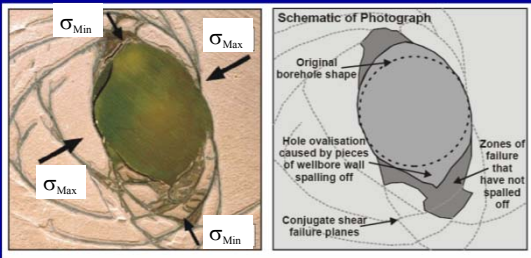
Min horizontal

## World Stress Map – $\sigma_{Hor}$ direction



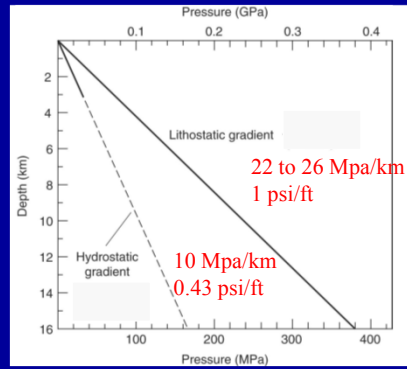
## Borehole Wall Breakouts and Stress

Horizontal Stresses



Caliper log measures the shape of the borehole

## Pressure/stress gradients



Overpressure =  
more than hydrostatic

Spindletop, 1901

Deepwater Horizon, 2010

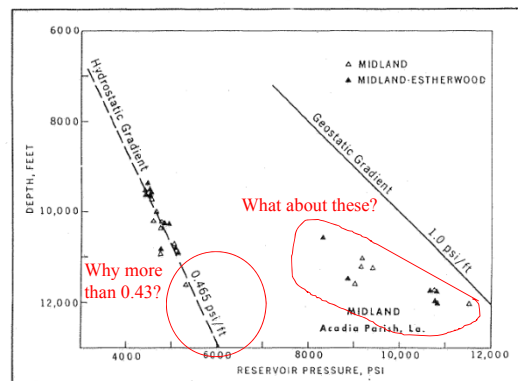
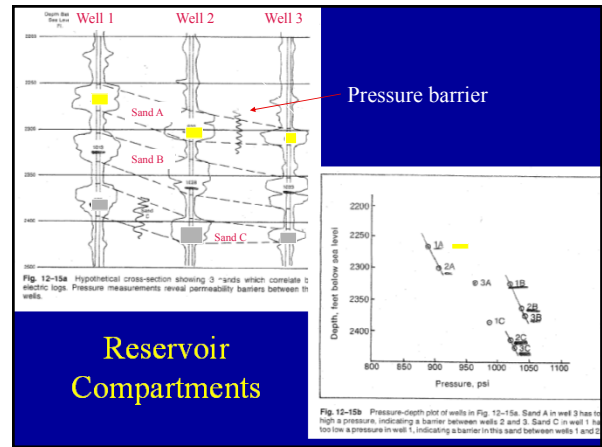
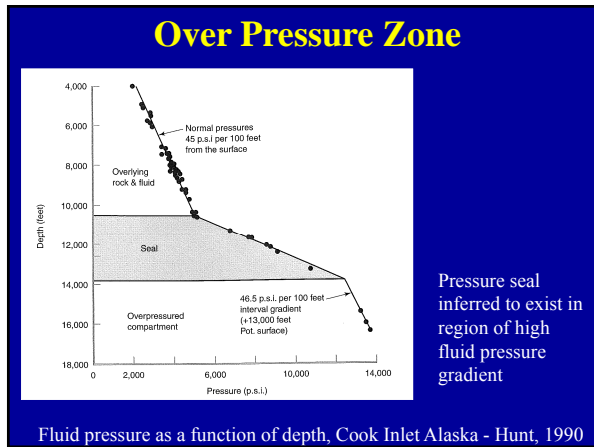
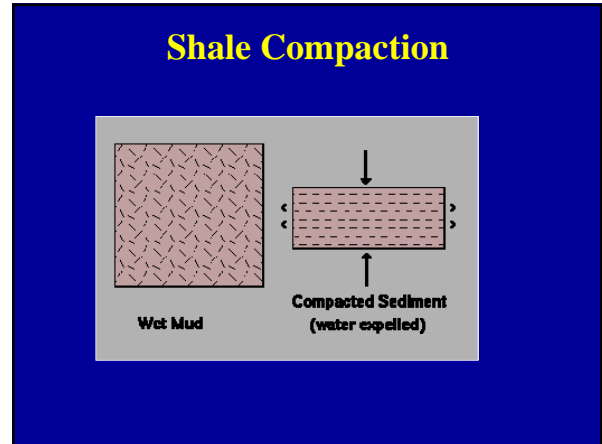
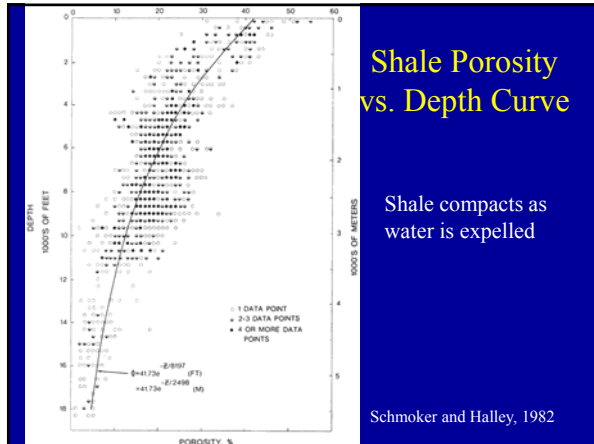
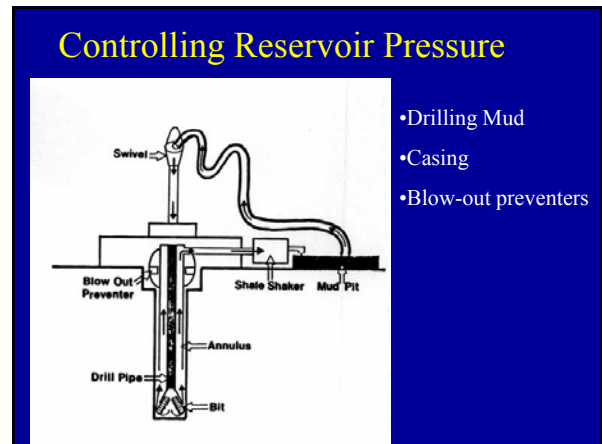


Fig. 12-28 Reservoir pressure vs depth, Midland field, Louisiana



- Characteristics of Overpressure Zones**
- Under-compacted shale
  - Low density, low sonic velocity
  - Rapid Drilling Rate
  - Low Thermal Conductivity, high T
  - Low Salinity

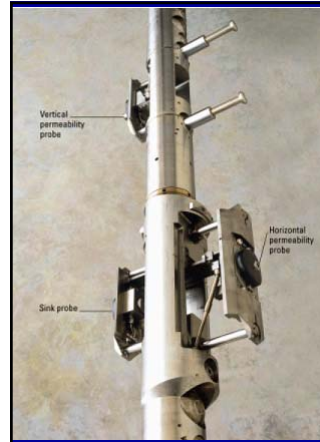


## Blow Out Preventers



How to measure formation pressure

Formation Tester Schlumberger



## How to measure reservoir pressure? Drill Stem Test

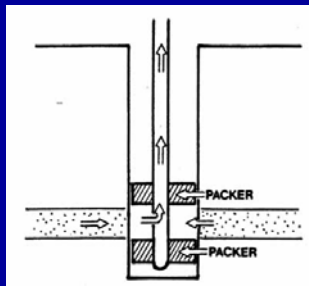
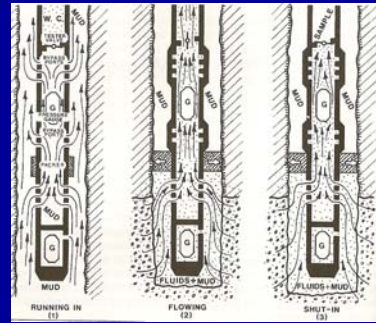


Figure 18-2 A drill stem test.

## Drill Stem Test (DST)



2. Initial Flow Period (IFP) removes effect of mud filtrate "supercharge"

3. Initial Shut-in is used to determine a reservoir Pressure (ISP)

Final Flow Period (FFP) is used to collect a fluid sample and create a pressure disturbance beyond any damaged zone.

Final Shut-in is used to test permeability, production rate and well damage

## Drill Stem Test Pressure Results

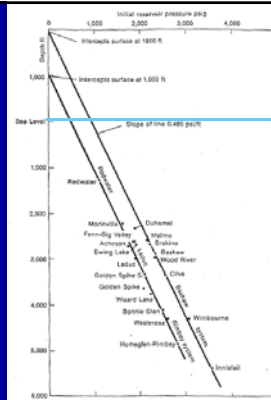
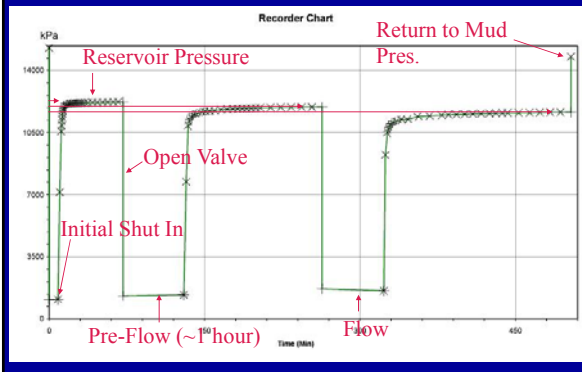


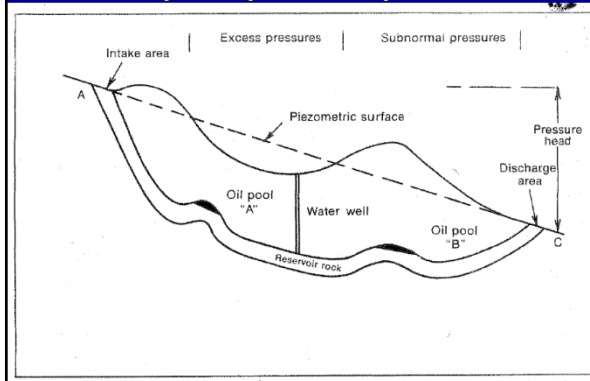
FIG. 12-4 Plot of initial reservoir pressure vs. depth of Leduc oil pools (A) (1987-1988)

Initial Reservoir Pressure  
Leduc Fields,  
Alberta (Canada)



Leduc #1 Gas flare

## Hydrodynamic System



SUBSURFACE PRESSURES

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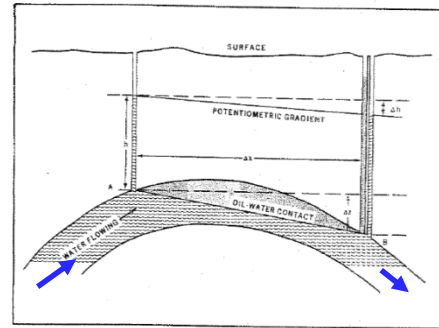
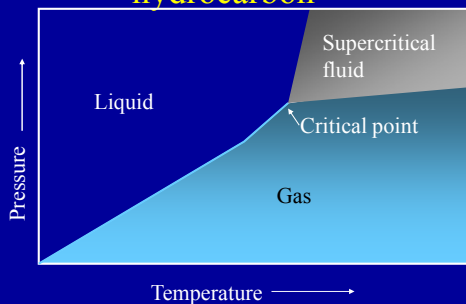


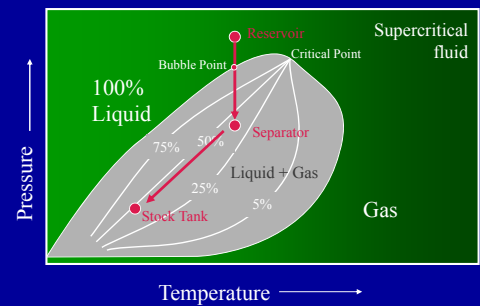
Fig. 12-20 Diagram showing why a flow results in a tilting of the oil-water contact. (From Hubbert)

## Phase Behavior for a single hydrocarbon

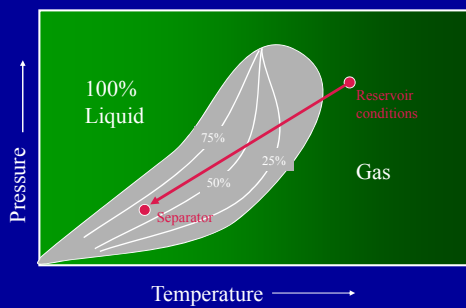


Supercritical: density like a fluid, viscosity like a gas

## Phase Behavior of Gas-Oil Mix



## Phase Behavior of Wet Gas or Condensate



## Summary

- $\sigma = \rho \cdot g \cdot z$
- Hydrostatic gradient = 0.43 psi/ft or 1 Mpa/km
- Lithostatic gradient = 1 psi/ft or 25 MPa/km
- Overpressure forms when water cannot escape
- Pressure gradient defines reservoir compartments
- Artesian aquifers can produce anomalous P
- Methods to control P during drilling
- Hydrodynamic reservoirs lead to tilted oil-water contacts
- Physical state of hydrocarbons depends on P-T regime
- Bringing oil to the surface cools and depressurizes it